Problem 22.38,42,46; 23.3,17,28 from MasteringPhysics with minor clarifications.

### 22.38 - Conducting Spherical Shell



A conducting spherical shell with inner radius $a$ and outer radius $b$ has a positive point charge $Q$ located at its center. The total charge on the shell is $-3 Q$, and it is insulated from its surroundings.

This means the net charge on the conductor is $-3 Q$, on both the inner and outer surface.

## Part A

Derive the expression for the electric field magnitude in terms of the distance $r$ from the center for the region $r<a$.

## Part B

Derive the expression for the electric field magnitude in terms of the distance r from the center for the region $a<r<b$.

## Part C

Derive the expression for the electric field magnitude in terms of the distance r from the center for the region $r>b$.

## Part D

What is the surface charge density on the inner surface of the conducting shell, $\rho_{\text {in }}$ ?

## Part E

What is the surface charge density on the outer surface of the conducting shell, $\rho_{\text {out }}$ ?

### 22.42 - Solid Conducting Sphere with Insulating Shell

A solid conducting sphere with radius $R$ carries a positive total charge $Q$. The sphere is surrounded by an insulating
shell with inner radius $R$ and outer radius $2 R$. The insulating shell has a uniform charge density $\rho$.

## Part A

Find the value of $\rho$ so that the net charge of the entire system is zero.

## Part B

If $\rho$ has the value found in part A, find the magnitude of the electric field, $E$, in the region $0<r<R$.

## Part C

If $\rho$ has the value found in part $A$, find the magnitude of the electric field in the region $R<r<2 R$.

## Part D

If $\rho$ has the value found in part A , find the direction of the electric field in the region $R<r<2 R$.

## Part E

If $\rho$ has the value found in part A, find the magnitude of the electric field in the region $r>2 R$.

### 22.46 - Conducting Tube

A very long conducting tube (hollow cylinder) has inner radius $a$ and outer radius $b$. It carries charge per unit length $+\alpha$, where alpha is a positive constant with units of $\mathrm{C} / \mathrm{m}$. A line of charge lies along the axis of the tube. The line of charge has charge per unit length $+\alpha$.

## Part A

Calculate the electric field in terms of $\alpha$ and the distance $r$ from the axis of the tube for $r<a$.

## Part B

Calculate the electric field in terms of $\alpha$ and the distance $r$ from the axis of the tube for $a<r<b$.

## Part C

Calculate the electric field in terms of $\alpha$ and the distance $r$ from the axis of the tube for $r>b$.

## Part D

What is the charge per unit length, $\alpha_{\mathrm{in}}$, on the inner surface of the tube?

## Part E

What is the charge per unit length, $\alpha_{\text {out }}$, on the outer surface of the tube?

## 23.3 - Moving Charges, Energy Methods <br> 

A small metal sphere, carrying a net charge of $q_{1}=-3.00 \mu \mathrm{C}$, is held in a stationary position by insulating supports. A second small metal sphere, with a net charge of $q_{2}=-7.30 \mu \mathrm{C}$ and mass $m_{2}=1.70 \mathrm{~g}$, is projected toward $q_{1}$. When the two spheres are $d_{0}=0.800 \mathrm{~m}$ apart, $q_{2}$ is moving toward $q_{1}$ with speed $v_{20}=22.0 \mathrm{~m} / \mathrm{s}$. Assume that the two spheres can be treated as point charges. You can ignore the force of gravity.

## Part A

What is the speed, $v_{21}$, of $q_{2}$ when the spheres are $d_{1}=0.430 \mathrm{~m}$ apart?

## Part B

How close, $d_{2}$, does $q_{2}$ get to $q_{1}$ ?

### 23.17 - Charge in a Uniform Electric Field

A charge of $q$ is placed in a uniform electric field that is directed vertically upward and that has a magnitude of $E$.

## Part A

What work, $W_{R}$, is done by the electric force when the charge moves a distance of $x_{1}$ to the right?

## Part B

What work, $W_{U}$, is done by the electric force when the charge moves a distance of $x_{2}$ upward?

## Part C

What work, $W_{45^{\circ}}$, is done by the electric force when the charge moves a distance of $x_{3}$ at an angle of $45.0^{\circ}$ downward from the horizontal?

### 23.28 - Electric Potential

At a certain distance from a point charge, the potential and electric field magnitude due to that charge are $V=4.98 \mathrm{~V}$ and $E=12.0 \mathrm{~V} / \mathrm{m}$, respectively. (Take the potential to be zero at infinity.)

## Part A

What is the distance, $d$, to the point charge?

## Part B

What is the magnitude of the charge, $q$ ?

## Part C

Is the electric field directed toward or away from the point charge?

