

# 1 Effect of the Coriolis Force on an Artillery Projectile

## 1.1 Lateral Deflection

A projectile is fired due east with an angle of inclination to the horizontal of  $\alpha$  and initial speed  $v_0$ . This takes place on the northern hemisphere at a latitude of  $\lambda$ . Show that the southward (lateral) deflection of the projectile can be approximated as

$$d = \frac{4v_0^3}{g^2} \omega \sin \lambda \sin^2 \alpha \cos \alpha \quad (1.1)$$

where  $g$  is the acceleration due to gravity near the surface of the earth, and  $\omega$  is the angular frequency of rotation of the earth. Neglect air resistance.

## 1.2 Is this an Important Effect for Artillery?

A howitzer has a muzzle velocity of about 680 m/s. If it fires a projectile due east with an angle of inclination of  $45^\circ$  and at a latitude of  $45^\circ$ , what will be the range,  $R$ , of this projectile and the southward deflection projectile,  $d$ ?

# 2 Effect of the Coriolis Force on a Projectile Going Straight Up and Down

A projectile is fired straight up and reaches a maximum height of  $h$ . This takes place on the northern hemisphere at a latitude of  $\lambda$ . (a) Show that the projectile lands distance of approximately

$$d = \frac{8}{3} \sqrt{\frac{2h^3}{g}} \omega \cos \lambda \quad (2.1)$$

from where it was launched, where  $g$  is the acceleration due to gravity, and  $\omega$  is the angular frequency of rotation of the earth. Neglect air resistance. (b) What is the direction that the projectile is deflected.